Mainstream traffic flow control on freeways using variable speed limits

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Abstract: Mainstream Traffic Flow Control (MTFC), enabled via variable speed limits, is a control concept for real-time freeway traffic management. The benefits of MTFC for efficient freeway traffic flow have been demonstrated recently using an optimal control approach and a feedback control approach. In this paper, both control approaches are reviewed and applied to a freeway network in a simulation environment. The validated network model used reflects an actual freeway (a ring-road), fed with actual (measured) demands. The optimal and feedback control results are discussed, compared and demonstrated to improve significantly the system performance. In particular, the feedback control scheme is deemed suitable for immediate practical application as it takes into account operational requirements and constraints, while its results are shown to be satisfactory. In addition, the control system performance was not very sensitive to variations of the parameters of the feedback controller. This result indicates that the burden associated with fine tuning of the controller may be reduced in the field.

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Keywords: freeway traffic control, mainstream traffic flow control, variable speed limits, feedback control, optimal control.

Resumo: Controle do Fluxo Principal (CFP), realizado via limites de velocidade variáveis, é um conceito de controle para o gerenciamento em tempo real do tráfego em rodovias. Os benefícios de CFP para a fluidez do tráfego foram demonstrados por pesquisas recentes que utilizaram uma abordagem de controle ótimo e uma abordagem de controle realimentado. Neste artigo, as duas abordagens de controle são revisadas e aplicadas a uma malha rodoviária em um ambiente de simulação. O modelo utilizado da malha rodoviária, que reproduz um anel viário real, foi validado e alimentado com demandas medidas em campo. Os resultados de controle ótimo e controle realimentado são discutidos e comparados, e produzem melhora significativa no desempenho do sistema. A estrutura de controle realimentado é considerada apropriada para a aplicação em campo, uma vez que considera requisitos e restrições operacionais, e apresenta resultados satisfatórios. Além disso, o desempenho do sistema de controle mostrou pouca sensibilidade a variações nos parâmetros do controlador realimentado. Este resultado indica que os esforços para sintonia do controlador em campo podem ser reduzidos.

Palavras-chave: controle de tráfego rodoviário, controle do fluxo principal, limites de velocidade variáveis, controle realimentado, controle ótimo.

1. INTRODUCTION

Traffic congestion cost reached US\$ 115 billion in urban areas in the USA in 2009 (Schrank *et al.*, 2010), while in Europe the traffic congestion cost was estimated at \in 100 billion in 2010 (European Comission, 2011). This is not surprising in view of the observed increasing road congestion extent around the globe and the fact that transport and mobility are one of the main drivers of the economical and technological development (Isermann, 2011).

Congestion forming on a freeway affects the nominal freeway capacity and throughput giving rise to an escalation of infrastructure degradation as a result of the absence of suitable traffic control measures that would counter and limit the congestion evolution. Thus, freeways need to be controlled for maximum efficiency, increased safety and reduced emission of pollutants. Indeed, transportation, in its different modes, is foreseen as one of the most challenging areas where future developments of automatic control are mostly expected (Isermann, 2011; IEEE, 2011).

A recent concept for freeway traffic flow control is Main-

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stream Traffic Flow Control (MTFC) as introduced by Carlson *et al.* (2010a, 2010b) using a nonlinear optimal control method. MTFC aims at directly influencing the freeway mainstream flow via an appropriate actuator, such as variable speed limits (VSLs), and may complement existing traffic control measures.

MTFC-like concepts had been investigated already in the 1960s (Greenberg e Daou, 1960; Gazis e Foote, 1969). With the increased interest in VSL systems, mainstream flow control strategies based on the use of VSLs were proposed and investigated for a variety of traffic application settings and control approaches, including optimal control (Alessandri et al., 1998), robust control (Chiang e Juang, 2008), feedback control (Zhang et al., 2006), modelpredictive control (Hegyi et al., 2005), distributed control (Popov et al., 2008), and rule-based control (Lin et al., 2004). Most of these VSL-based strategies, however, are not deemed sufficiently mature for a practical application, see Carlson et al. (2011a). A noteworthy exception seems to be the recent SPECIALIST effort (Hegyi e Hoogendoorn, 2010) which demonstrated that mainstream traffic flow regulation via VSLs actually works in practice, albeit based on a feed-forward approach. The reader is referred to Carlson et al. (2011a) for more details on past work.

In an attempt to circumvent the practical limitations of some of the previous methods, Carlson *et al.* (2011a) proposed, based on the same MTFC application concept of Carlson *et al.* (2010a, 2010b), a simple, yet efficient VSLbased MTFC feedback cascade controller that is deemed suitable for ready field implementation. This paper demonstrates the use of the two controllers developed by Carlson

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et al. (2010a, 2010b, 2011a) for the MTFC on freeways via VSLs. A new set of simulation experiments of an actual freeway (a ring-road) using actual (measured) demands demonstrates the controllers' main features under realistic conditions – in fact the closest to reality one can reach before field implementation. Furthermore, since fine-tuning of the feedback controller is an unavoidable task in practice, the performance of the closed-loop system is evaluated with respect to variations of the parameters of the controller and is shown to exhibit low sensitivity to these variations.

In the next section, some basic insights related to freeway traffic control are presented, and the MTFC concept is reviewed; in addition, the essentials of the METANET simulator (Messmer e Papageorgiou, 1990; Carlson *et al.*, 2010b) used for the evaluation of the controllers is outlined. Section 3 recapitulates the optimal control strategy implemented within the AMOC optimal control tool (Kotsialos *et al.*, 2002b; Carlson *et al.*, 2010b) and the MTFC feedback cascade controller designed by Carlson *et al.* (2011a). The optimal control and feedback control strategies are compared and have their efficiency evaluated in Section 4. Finally, Section 5 concludes the paper and comments on further research on the subject.

2. BACKGROUND

2.1. The fundamental diagram

The traffic flow states may be approximated by the *fundamental diagram*, which is usually represented as a flow q(veh/h) versus density ρ (veh/km) diagram, as in Figure 1(a). The point of maximum flow in the diagram corresponds to the *capacity flow* q_{cap} at the freeway location where the diagram was obtained, while the corresponding traffic density value is called the *critical density* ρ_{cr} . The mean speed of a particular traffic state on the flow-density diagram is the slope of the line that connects the particular traffic state point with the origin. A *critical (mean) speed* v_{cr} is associated to the state of capacity flow.

2.2. Congestion-caused infrastructure degradation

A bottleneck on a freeway is a location where the flow capacity $q_{\rm cap}^{\rm up}$ upstream is higher than the flow capacity $q_{\rm cap}^{\rm down}$ downstream of the bottleneck location (Figure 2(a)). If the arriving flow $q_{\rm in}$ is higher than $q_{\rm cap}^{\rm down}$, the bottleneck is activated, i.e., congestion is formed. Congestion forming at an active bottleneck has two detrimental effects on freeway capacity and throughput (Papageorgiou e Kotsialos, 2002):

- Capacity drop (CD) at the congestion head, i.e., an active bottleneck outflow q_{out} that may be 5-25 % lower than the nominal capacity q_{cap}^{down} , see, e.g., Chung *et al.* (2007). A main contributing factor for CD occurrence is deemed to be the acceleration of vehicles while exiting the congested area; and
- Blocking of off-ramps (BOR): vehicles that are bound for exits upstream of the active bottleneck, are also delayed due to the blocking of the corresponding off-ramps by the congestion body, while the offramp flow is reduced.

2.3. The MTFC concept

The basic idea of MTFC is to regulate the mainstream traffic flow sufficiently upstream (some 500 m) of (otherwise) active bottlenecks, so as to avoid the CD (since vehicles will have accelerated before reaching the bottleneck area) and establish maximum bottleneck throughput (Figure2(b)). The bottleneck of Figure 2(b) is not activated (and no MTFC is needed) as long as $q_{\rm in} \leq q_{\rm cap}^{\rm down}$, in which case $q_{\rm out} \approx q_{\rm in}$. If $q_{\rm in}$ grows bigger than the bottleneck capacity $q_{\rm cap}^{\rm down}$, the bottleneck would be activated in absence of control as in Figure 2(a), and $q_{\rm out}$ would be reduced due to CD; while MTFC can implement a controlled mainstream flow q_c , such that $q_{\rm out}$ is equal to $q_{\rm cap}^{\rm down}$. Clearly, the mainstream congestion cannot be avoided via MTFC, because







 $q_{\rm in} > q_{\rm cap}^{\rm down}$ (otherwise MTFC would not intervene), but the congestion outflow in the MTFC case is higher than in the no-control case, because the capacity drop is avoided; hence the controlled congestion is space-time shorter than in the no-control case (and thus the BOR effect is accordingly reduced). Further details on the benefits of MTFC can be found in Carlson *et al.* (2010a, 2010b, 2011a).

In this paper, variable speed limits (VSLs) are used as an MTFC actuator to impose the controlled flow q_c on the freeway mainstream. The use of VSLs requires consideration of several implementation issues that were detailed by Carlson *et al.* (2010a, 2011a).

2.4. Traffic flow simulation model (METANET)

A validated macroscopic second-order traffic flow model included in the METANET freeway traffic flow simulator (Messmer e Papageorgiou, 1990) that incorporates VSL control measures (Carlson *et al.*, 2010b) was used in this work.

The freeway network is represented by a directed graph, whereby the links of the graph represent freeway stretches with uniform characteristics. The nodes of the graph are placed at locations where a major change in road geometry occurs, as well as at junctions and on-/off-ramps. The time and space arguments are discretized. The time step is denoted by T (typically T = 10 s). A freeway link m is divided into N_m segments of equal length L_m (typically $L_m = 500$ m). The traffic in each segment i of link m at discrete time t = kT, k = 0, 1, ..., is macroscopically characterized via the following variables: the traffic density $\rho_{m,i}(k)$ (veh/km/lane) is the number of vehicles in segment i of link *m* at time t = kT divided by L_m and by the number of lanes λ_m ; the mean speed $v_{m,i}(k)$ (km/h) is the mean speed of the vehicles in segment *i* of link *m* at time t = kT; and the traffic volume or flow $q_{m,i}(k)$ (veh/h) is the number of vehicles leaving segment i of link m during the time period $\left[kT, (k+1)T\right)$ divided by T.

The density and mean speed are state variables calculated from the conservation equation and a dynamic speed equation, respectively (see Messmer and Papageorgiou (1990)); flows are calculated from

$$q_{m,i}(k) = \rho_{m,i}(k) v_{m,i}(k) \lambda_m.$$
(1)

The dynamic speed equation includes a static speeddensity relationship, which is equivalent to a fundamental diagram, that incorporates the impact of variable speed limits. Particular VSL values are reflected in corresponding link-specific VSL rates $b_m(k)$ that prevail, by definition, during [kT, (k+1)T), at link m (or a cluster of links). The VSL rate b_m is approximately equal to the displayed VSL divided by the legal speed limit without VSL. The VSL rates are control variables with $b_m(k) \in [b_{\min,m}, 1.0]$ where $b_{\min,m}$ is a lower admissible bound, while $b_m = 1.0$ means no VSL displayed. The kind of changes incurred to the fundamental diagram via the VSLs may be viewed in Figure 1(b) and are attributed to the reduced speeds at undercritical states of traffic (i.e., states to the left of the critical density on the fundamental diagram) and the homogenizing effect of the speed limits (see, e.g., Papageorgiou *et al.* (2008)).

METANET also includes appropriate modeling equations for network nodes, that involve, among others, the dynamics of origin (e.g., on-ramp) queues w_o ; for further details, see Messmer and Papageorgiou (1990).

The nonlinear macroscopic traffic flow model outlined above may be formulated as a discrete-time state-space model for the entire freeway network:

$$\mathbf{x}(k+1) = \mathbf{f}[\mathbf{x}(k), \mathbf{u}(k), \mathbf{d}(k)], \quad \mathbf{x}(0) = \mathbf{x}_0 \qquad (2)$$

with **x** the state vector, **u** the control vector and **d** the disturbance vector. The state vector consists of the densities $\rho_{m,i}$ and the mean speeds $v_{m,i}$ of every segment *i* of every link *m*, and the queues w_o of every origin *o*. The control vector consists of the VSL rates b_m of every link *m* where VSL is applied (otherwise $b \equiv 1.0$). The disturbance vector consists of the demand d_o at every origin *o* and the turning rates β_n^m at every bifurcation node *n* towards out-link *m*.

2.5. VSLs as an MTFC actuator

The applicability of MTFC via VSLs relies mainly on the utilization of two aspects of the effect of VSLs on the aggregate traffic flow behavior (Carlson *et al.*, 2010b, 2011a):

- If the mainstream demand q_{in} (Figure 2(b)) arriving from upstream is lower than the VSL-induced capacity, then the application of VSL will temporarily (for the duration of the traffic state transition triggered by the VSL) decrease the mainstream flow arriving in the bottleneck area; after this transition period, the outflow from the VSL application area returns to values equal to the upstream arriving demand q_{in} (Figure 1(b)). This temporary flow reduction may be exploited to temporarily hold back traffic flow in order to retard the onset of congestion at the downstream bottleneck; and
- Sufficiently low VSL values lead to accordingly lower flow capacity in the fundamental diagram (Figure 1(b)). This implies that, if the mainstream demand $q_{\rm in}$ (Figure 2(b)) arriving from upstream is higher than the VSL-induced capacity, then the VSL application area becomes an active mainstream bottleneck that limits the area's outflow $q_{\rm c}$ to values corresponding to the (lower) VSL-induced capacity; this provides the possibility to apply a more durable mainstream flow control, which persists even after the transition period. Thus, a controllable mainstream of a bottleneck location to avoid its activation and the related reduction of throughput because of the capacity drop.

The above two aspects cannot be associated to a specific VSL range in a freeway, since they depend also on the arriving demand q_{in} . Additionally, lower VSL rates shift the critical density of the fundamental diagram towards higher values (Figure 1(b)).

3. OVERVIEW OF MAINSTREAM TRAFFIC FLOW CONTROLLERS

In this section two mainstream traffic flow controllers are reviewed. First, the optimal control approach is reviewed and then the cascade feedback controller.

3.1. Nonlinear constrained optimal control (AMOC software tool)

The freeway network traffic control problem may be formulated as a discrete-time nonlinear dynamic optimal control problem with constrained control variables over a given optimization horizon K_p , and is incorporated in the open-loop optimal control tool AMOC (Kotsialos *et al.*, 2002b). The general formulation of the optimal control problem reads:

Given disturbance predictions $\mathbf{d}(k)$, $k = 0, 1, \dots, K_{\rm P} - 1$,

and the initial state $\mathbf{x}(0) = \mathbf{x}_0$; minimize

$$J = \mathcal{G}\left[\mathbf{x}(K_{\mathrm{P}})\right] + \sum_{k=0}^{K_{\mathrm{P}}-1} \varphi\left[\mathbf{x}(k), \mathbf{u}(k), \mathbf{d}(k)\right]$$
(3)

subject to (2) and $b_{\min,m} \le b_m \le 1.0$.

The chosen cost criterion is the total time spent (TTS) by all vehicles in the network, including the waiting time experienced in the ramp queues. Moreover, a low-weighted term may be added to penalize (abrupt) time variations of the optimal VSL rate trajectories (Carlson *et al.*, 2010b).

The AMOC solution consists of the optimal VSL rate and state variable values within the horizon $K_{\rm p}$ that minimize the TTS. Common VSL rates can be considered for clusters of links.

The optimal control problem delivers ideal solutions in a simulation environment due to the "perfect" model, the exact knowledge of (future) disturbances (demands and turning rates) and the lack of some VSL constraints. Clearly, these solutions cannot be outperformed (in simulation) by any other control strategy but may be used to assess the efficiency of other (simpler) strategies under different scenarios. In practice, unless the optimal control strategy is cast in a model-predictive framework (Papamichail *et al.*, 2010), the solution from the optimal control approach becomes suboptimal due to various inherent uncertainties.

3.2. Feedback controller

The control problem implied within Figure 2(b) is to regulate the traffic density ρ_{out} (the control output) via appropriate real-time changes of the mainstream flow q_c , which are enabled via the display of appropriate VSLs upstream of the bottleneck location with the VSL rate *b* as the control input.

The basis for the design of the feedback MTFC via VSLs is a discrete-time linearized model (Carlson *et al.*, 2011a):

$$\frac{\Delta \rho_{\text{out}}\left(z\right)}{\Delta b\left(z\right)} = K \cdot K' \frac{\tau}{z + \tau - 1} \cdot \frac{z - \alpha}{z - \beta} \tag{4}$$

with α , β , τ , K' > 0 and K > 0 being model parameters, and $0 < \beta < \alpha \le 1$; *z* the discrete-time complex variable; $\Delta \rho_{\text{out}}$ the density variation at the bottleneck location



actuator

due to a variation Δb at the application area.

Figure 3 depicts the MTFC feedback cascade structure designed by Carlson *et al.* (2011a). The internal loop in Figure 3 is affected by the VSL rate *b* delivered by the secondary controller that will determine the outflow q_c of Figure 2(b). The secondary controller was designed as an integral (I) regulator:

$$b(k) = b(k-1) + K_{\mathrm{I}}e_{\mathrm{q}}(k) \tag{5}$$

with $K_{\rm I}$ the integral gain and $e_{\rm q}(k) = \hat{q}_{\rm c}(k) - q_{\rm c}(k)$ the flow control error.

The flow q_c measured downstream of the application area is used as a reference for the primary controller and is fed back and compared to the reference flow \hat{q}_c delivered by the primary controller. The primary controller uses the measured density ρ_{out} at the bottleneck area and compares it with the set-point density $\hat{\rho}_{out}$, which is set equal to the critical density ρ_{cr} for throughput maximization. The primary controller was specified to be a proportional-integral (PI) regulator:

$$\hat{q}_{c}(k) = \hat{q}_{c}(k-1) + (K'_{P} + K'_{I})e_{\rho}(k) - K'_{P}e_{\rho}(k-1) \quad (6)$$

with $K'_{\rm I} = K'_{\rm P}$ the integral and proportional gains of the controller, respectively, and $e_{\rho}(k) = \hat{\rho}_{\rm out} - \rho_{\rm out}(k)$ the density error. For more details about the controller design, tuning and operation, see Carlson *et al.* (2011a).

3.2.1. VSL application aspects

This section summarizes some practical VSL implementation aspects detailed in Carlson et al. (2011a). To start with, VSLs can only take discrete values in practice. Therefore, a set of admissible discrete VSL rates $b \in \{0.1, 0.2, \dots, 1.0\}$ is defined and the discrete VSL rate to be applied is obtained by rounding off the VSL rate b(k) delivered by the control strategy (5). As further constraints, the difference between two consecutive posted VSL rates at the same variable message sign (VMS) is limited to 0.2. Similarly, the difference between the posted VSL rates at two consecutive VMSs is also limited to 0.2. Furthermore, a constant VSL rate of 0.9 is applied in the acceleration and bottleneck areas whenever the MTFC via VSL system is active. Finally, for traffic safety reasons, additional VSLs may be activated within and upstream of the controlled congestion in a way that vehicles driving towards the congestion tail encounter gradually decreasing VSLs. These practical aspects are only considered when applying feedback concepts, not with AMOC optimal control results (see Section 3.1).

4. SIMULATION RESULTS

After introducing the freeway network to be studied, different control scenarios are discussed in this section. First, the network is simulated without any control measure, as a base reference, using the METANET simulator. Next, the network is tested under optimal MTFC via VSLs, as an upper limit of achievable performance under ideal conditions, using the AMOC optimal control tool. Then, the freeway is simulated with feedback cascade MTFC via VSLs, with and without the constraints described in Section 3.2.1, using the METANET simulator. The simulated scenarios and resulting TTS are summarized in Table 1. Finally, an additional set of simulations with the feedback cascade controller is run to evaluate the sensitivity of system performance with respect to variations in the controller's parameters.

4.1. The Amsterdam ring-road

For this study, the counter-clockwise direction of the Amsterdam ring-road A10 is considered (Figure 4). This freeway is about 32 km long and has 21 on-ramps, including the freeway-to-freeway junctions with A1, A2, A4 and A8, and 20 off-ramps, including connections with A1, A2, A4 and A8. The merge area of A1 (OA1) with A10 at L107 is the main recurrent active bottleneck of the network. The model parameters were determined from validation of the network traffic flow model against actual data, see Kotsialos *et al.* (2002a); while the VSL-specific parameters were chosen such that the VSL-induced capacity $q_{cap,m}^{*}(b_m)$ is not higher than the non-VSL capacity $q_{cap,m}$ for any VSL value (Carlson *et al.*, 2010a), as sketched in Figure 1(b).

The ring-road was studied for a time horizon of 4 h using measured demands from the site. For the controlled scenarios, the frequency of VSL changes is determined by the control period. In this paper the VSL rates are allowed to change every $T_c = 60$ s with $b_{\min,m} = 0.2$ (see Carlson *et al.* (2011a, 2013) for details on the choice of the control period). The simulation time step is T = 10 s.

4.2. No-control case

When simulating the network without any control measures, heavy congestion appears in the freeway and large queues are built in some on-ramps. The related density and queue profiles are displayed in Figure 5(a-b). Congestion is formed shortly after the beginning of the simulation (Figure 5(a)) as a consequence of the excessive demand and the absence of control measures. This traffic jam originates at the junction of A1 with A10 and propagates upstream, blocking A4 and a large part of the A10-West. The density at the bottleneck area (merge area of A1; first segment of L107) is shown by the black curve in Figure 6(a) and is clearly overcritical (the critical density is $\rho_{cr} = 32$ veh/km/lane) for most of the simulation duration. The corresponding flow at the bottleneck area of around 5400 veh/h is shown in Figure 6(b), and is below capacity ($q_{cap,L107} = 5900$ veh/h) because of a capacity drop of around eight percent.

After the first traffic jam is partially dissolved, a new one appears leading to more severe congestion. This strong congestion keeps the A4 entrance to the A10 blocked, which results in the queues at the freeway-to-freeway on-ramp of A4 and at the surrounding on-ramps (Figure 5(b)). Likewise, off-ramp outflows are affected by the congestion mounting upstream, but further details on this issue are postponed to the subsections that follow. The TTS for this scenario is equal to 14,163 veh-h. The described no-control simulation results are very similar to the corresponding real afternoon-peak traffic conditions (Kotsialos *et al.*, 2002a).

Strategy	Description	TTS (veh·h)	%
	The network is simulated without any control measures using the		
No-control	METANET simulator.	14,163	-
	The network is simulated for optimal MTFC via VSLs using the AMOC		
Optimal Control (AMOC)	optimal control tool.	8,675	-38.8
	The network is simulated for feedback MTFC via VSLs using the		
Feedback Control (FB)	METANET simulator without any constraints.	9,315	-34.2
	The network is simulated for feedback MTFC via VSLs using the		
Feedback Control	METANET simulator with discretized VSL rates, limited VSL rate		
(with constraints)	variation, and $b_{L105-L107} = 0.9$	9,184	-35.2
Feedback Control	The network is simulated for feedback MTFC via VSLs using the		
(with constraints and	METANET simulator with discretized VSL rates, limited VSL rate		
safety speed limits)	variation, $b_{1,105,1,107} = 0.9$ and safety speed limits.	9,513	-32.8

Table 1. Summary of Simulated Control Scen
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Figure 5. No-control: (a) network density and (b) ramp queues; optimal control: (c) network density and (d) ramp queues; and feedback control: (e) network density and (f) ramp queues



Figure 6. All scenarios: (a) density and (b) flow at the bottleneck location

4.3. Nonlinear optimal control (AMOC)

Next, MTFC via VSLs is applied using nonlinear optimal control (AMOC). In contrast to Carlson *et al.* (2010a), only one cluster of links, L101-L102, is considered in this investigation, i.e., VSLs are applied locally in the area near the bottleneck location, similarly to what is done with local feedback in the next section.

The resulting TTS value for this scenario is equal to

8,675 veh·h, which is a 38.8 percent improvement compared to the no-control case. The related density and ramp queue profiles are shown in Figure 5(c-d), while the optimal VSL rate trajectory is shown in Figure 7(a). The density and flow at the bottleneck area are shown by the dark grey curves in Figure 6.

Figure 5(c) indicates that there are two traffic jams forming, but, in contrast to the no-control case, these queues are shorter in space and time, and less intense. The detailed plots in Figure 6 show that up to t = 0.2 h the traffic density at the A1 merge area is maintained about its critical value and flow is near capacity, while a congestion is formed a few segments upstream (Figure 5(c)). These controlled congestions are initially formed at L101-L102, i.e., upstream of the A1/A10-junction bottleneck, due to the holding back of traffic via appropriate (optimal) MTFC via VSLs, in contrast with the no-control case when congestion is formed at the bottleneck area. Indeed, the strong VSL control action applied at L101-L102 indicates that these links are used as an application area while L105 acts as an acceleration area so as to avoid the capacity drop at the merge area of A1 with A10. However, this VSL control action at L101-L102 is quickly released, and a light congestion starts forming at the merge area of A1, despite the fact that this congestion could have been completely avoided by MTFC via lower VSLs. Instead, AMOC's control action results in the use of the space at the merge area and also at some of the upstream links to store more vehicles via higher densities at these locations (Figure 5(c)). In this way, the congestion length and intensity is managed by the optimal control strategy so as to reduce the BOR effect farther upstream. This more than counterbalances the reduction of throughput due to the short-term capacity drop at the merge area of A1 (Figure 6(b)), and the reduced outflow of off-ramps immediately upstream of the bottleneck. This last aspect will be discussed in more detail in the next section.

At around t = 0.7 h, VSL is once again strongly applied at L101-L102 reaching its lower bound for about half an hour and bringing back the bottleneck area density to around the critical density, before the reduction in demand allows for a short period of undercritical densities. The interpretation of the second half of the simulation is similar to the first period and is omitted.

4.4. Cascade feedback control (FB)

Cascade feedback MTFC via VSLs is now applied as described in Section 3.2. First, the VSL rate b(k) delivered by the control law (5) is applied at L101-L102, which corresponds to the VSL application area, without any restriction. The density measurement is taken from the first segment of L107, where the merge from A1 occurs, while the flow measurement is taken from the first segment of L105, immediately downstream of the application area and the exit to A1. The critical density at the bottleneck location is used as the set-point for the primary controller and is $\hat{\rho}_{out} = 32$ veh/km/lane. The used controller gains are $K'_{\rm P} = 38$ km/h and $K'_{\rm I} = 9$ km/h for the primary controller, and $K_{\rm I} = 0.0015$ h·lane/veh for the secondary controller.

The resulting TTS for this scenario is equal to 9,315 veh·h, which is a 34.2 percent improvement compared to the no-control scenario. The related density and ramp queue profiles are shown in Figure 5(e-f), while the VSL rate trajectory at L101-L102 is shown in Figure 7(b). The density and flow at the bottleneck area are shown by the light gray curves in Figure 6.

Once again, it can be seen in Figure 5(e) that there are two congestions forming. In contrast to the two previous scenarios, the bottleneck congestion and, consequently, the capacity drop are completely avoided in the merge area of A1 (Figure 6(a)) as density remains around the set-point



Figure 7. VSL rate trajectories: (a) optimal control; (b) feedback control without constraints; and (c) feedback control with constraints

value $\hat{\rho}_{out} \approx \rho_{cr,L107}$ marked by the dotted line in the figure.

The VSL rates at the application area (Figure 7(b)) are seen to go as low as 0.2, so as to hold back traffic. Because feedback maintains the density at the bottleneck around the set-point, the flow at that location (Figure 6(b)) is higher for feedback than for optimal control when the latter allows for a merge congestion to form.

Despite the fact that feedback has a higher flow at the bottleneck location than AMOC, the feedback control TTS is 5 percent higher (Table 1). A reason why feedback has a worse performance than AMOC is the BOR effect on farther upstream ramps. Note that, despite the local application of MTFC via VSLs at links L101-L102, AMOC acts with global network knowledge. This renders AMOC capable of managing the densities upstream of the bottleneck location in the most efficient way, so as to maximize throughput through all network off-ramps.

To better illustrate the BOR effect, Figure 8 shows, as an



Figure 8. Optimal and feedback control: time-accumulated outflows at off-ramp DA4

example, the time-accumulated outflow at the off-ramp to the A4 freeway that is clearly covered by both congestions forming in the no-control and feedback scenarios, but only covered by the first congestion in the AMOC case. At around t = 0.5 h, the AMOC curve departs from the feedback control curve, which indicates that more cars exited through DA4 in the AMOC case. The curves catch up with each other again at around t = 2.5 h, but just after, the exit flow is again higher with AMOC.

The practicality of the feedback control approach presented depends on the consideration of some operational requirements and constraints as introduced in Section 3.2.3. The VSL-induced critical density resulting from the VSL rate of 0.9 at the acceleration and bottleneck areas (L105-L107) is used as the set-point for the primary controller and is $\hat{\rho}_{out} = 34$ veh/km/lane. The resulting TTS for this scenario is equal to 9,184 veh·h, which is a 35.2 percent improvement compared to the no-control scenario and slightly better than the previous scenario. The detailed results are omitted, as the differences with the previous scenario are minor. The VSL rate trajectories at L101-L102 and L105-L107, however, are shown in Figure 7(c) and describe a similar trajectory as in the previous scenario while exhibiting discrete values as discussed in Section 3.2.3.

Typically, for safety reasons, additional VSLs may be applied upstream of the application area (see Section 3.2.3). In this case, the resulting TTS is equal to 9,513 veh h, which is a 32.8 percent improvement cc^{--} pared to the no-

control scenario and slightly worse than the previous scenarios. This efficiency reduction is considered minor in face of the potential safety benefits. Further details on the implementation of the operational restrictions can be found in Carlson *et al.* (2011a).

4.5. Sensitivity to variations of the parameters of the feedback controller

The gains used for the feedback controller in Section 4.4 were obtained using the zone-based method (Ellis, 2004; Carlson *et al.*, 2011a). However, given the complexity of the system being dealt with, it is likely that a fine-tuning will still be required. Fine-tuning may be a complicated and time-consuming task, and, having a controller that exhibits a good performance for a range of its parameter values, may reduce the associated task burden. This is related to the problem of controller fragility analysis (Alfaro, 2007), i.e., how the performance of a control system is affected by variations of the parameters of the controller.

The performance of the system was evaluated by repeating the first simulation of Section 4.4 for different combinations of parameters with values around the "nominal" values obtained in the first tuning of the controller. The sets used were $K'_{\rm P} \in \{34, 35, ..., 38, ..., 42, 43\}$ km/h and $K'_{\rm I} \in \{4, 5, ..., 9, ..., 13, 14\}$ km/h for the primary controller, and $K_{\rm I} \in \{0.0010, 0.0011, ..., 0.0015, ..., 0.0010, 0.0020\}$

0.0019, 0.0020} h·lane/veh. The worst performance in terms of TTS resulted in a TTS of 9596 veh-h, i.e., an improvement of 32.2 percent, obtained with $K'_{\rm P} = 33$ km/h, $K'_{\rm I} = 14$ km/h and $K_{\rm I} = 0.0010$ h·lane/veh. The best performance resulted in a TTS of 9258 veh-h, i.e., an improvement of 34.7 percent, obtained with $K'_{\rm P} = 37$ km/h, $K'_{\rm I} = 8$ km/h and $K_{\rm I} = 0.0020$ h·lane/veh. In both cases the improvement is very close to the one obtained in Section 4.4 of 34.2 percent. Figure 9(a) shows the typical plot shape that was obtained for parameter sets where K'_{I} was kept fixed (in the figure, $K'_1 = 11$ km/h) and the other two parameters $(K'_{P} \text{ and } K_{I})$ were varied as defined previously. An improvement is seen in the performance for increasing $K'_{\rm P}$ and $K_{\rm I}$ with an associated slightly more nervous control action (not shown), though still within acceptable limits, i.e., the impact on traffic within and upstream of the application area is not compromised. In other words, the more



Figure 9. Variation of the parameters of the feedback controller (a) TTS for $K'_{I} = 11$ km/h and combination of values for K'_{P} and K_{I} (b) density at the bottleneck location for the "nominal", worst and best cases

nervous control action delivered by the controller is not reflected by more frequent variations of the discretized speed limit than exhibited in Figure 7(c). In Figure 9(b) the density at the bottleneck area is shown for the worst and best cases as well as for the "nominal" case. There is no significant difference between the nominal and best cases. The worst case on the other hand, responds slightly slower and shows some stronger variations around the set-point.

5. CONCLUSIONS

This paper demonstrated the use of automatic control methods applied to the mainstream traffic flow control (MTFC) on freeways. Two approaches, based on optimal and feedback control methods, respectively, were reviewed and tested in simulation using a validated macroscopic secondorder traffic flow simulator and a large-scale network model with realistic demands. Control was applied locally, and the results have shown that feedback control performs satisfactorily. The performance of the closed-loop system was shown to have low sensitivity to variations of the parameters of the feedback controller, indicating that the possibly necessary fine-tuning in field applications is likely to not be too demanding. The feedback controller is deemed to be suitable for applications in the field.

Further improvements in total time spent could be obtained by the extension and integration of these controllers with other freeway control strategies and measures at the local and network-wide levels. Ongoing research is addressing these problems and preliminary results can be found in Carlson *et al.* (2011b, 2012). A field test of the presented feedback strategy should be attempted in the near future.

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